

Integration by parts

"reverse product rule"

$$\int u \frac{dv}{dx} dx = uv - \int v \frac{du}{dx} dx \quad \text{or} \quad \int u dv = uv - \int v du$$

Find the integral of

$$\int \underbrace{x}_{u} \underbrace{\sin x}_{\frac{dv}{dx}} dx = -x \cdot \cos x - \int -\cos x dx$$

1) make the "u" function
the polynomial /

Simpler of the
2 options

$$= \underbrace{-x}_{u} \underbrace{\cos x}_{v} + \sin x + C$$

$$f'(x) = +x \sin x - 1 \cos x + \cos x$$

Integration by parts

$$\int u \frac{dv}{dx} dx = uv - \int v \frac{du}{dx} dx \text{ or } \int u dv = uv - \int v du$$

Find the integral of

$$\int \underbrace{\ln x}_u \cdot \underbrace{1}_{\frac{dv}{dx}} dx$$

$$\int \ln x dx = \int \underbrace{1}_u \cdot \underbrace{\ln x}_{\frac{dv}{dx}} dx \quad \text{lolz}$$

$$= 1 \cdot \int \ln x dx - \int 0 \cdot \ln x dx$$

$$\ln(x) \cdot x - \int x \cdot \frac{1}{x} dx$$

$$x \ln x - \int 1 dx$$

$$\boxed{x \cdot \ln x - x + C}$$

$$x \cdot \frac{1}{x} + 1 \cdot \ln x - 1$$

$$1 + 1 \cdot \ln x - 1$$

Integration by parts

$$\int u \frac{dv}{dx} dx = uv - \int v \frac{du}{dx} dx \quad \text{or} \quad \int u dv = uv - \int v du$$

Find the integral of $\int \underbrace{e^x}_u \underbrace{\cos x}_{dv/dx} dx = e^x \cdot \sin x - \int \underbrace{\sin x}_{dv/dx} \cdot \underbrace{e^x}_u dx$

$$\int e^x \cos x dx = e^x \sin x + e^x \cos x - \int e^x \cos x dx$$

$$2 \int e^x \cos x dx = e^x (\sin x + \cos x) + \int e^x \cos x dx$$

2

2

$$-e^x \cdot \cos x - \int -\cos x \cdot e^x dx$$

$$(-e^x \cdot \cos x + \int e^x \cos x dx)$$

$$\int e^x \cos x dx = \frac{e^x}{2} (\sin x + \cos x) + C$$