









Weight at birth (5:52am): 10 lb 1 oz 161 oz
(5 oz)
12 hrs later (5:52pm): 9 lb 12 oz 156 oz
(5 oz)
12 hrs later (5:52am + 1 day): 9 lb 7 oz 151 oz
(5 oz)
12 hrs later (5:52pm + 1 day): 9 lb 2 oz 146 oz



NICU

Is this an arithmetic sequence?

+, -

Y, N

Class idiosyncracies:

- *Tutorials M-Th 7:30am (any time in morning is good!)
- *Deposit phone in shoe locker in order to access bathroom pass
- *Tutorial videos + e-mail message with question = 10 bonus points on homework

A penny doubled for 3 weeks and you keep the final payment only,

or...
 $\$0.01$, $\$0.02$, $\$0.04$
today tomorrow

\$10,000

geometric

Which option would you choose?

$$u_n = u_1 \cdot r^{n-1}$$

Today's learning objective:

By the end of class, I will be able to distinguish arithmetic sequences from geometric and calculate n-th terms for each.

Today's language objective:

- Arithmetic sequence
- Geometric sequence
- n-th term
- common difference
- common ratio

The diagram shows the formula $u_n = u_1 r^{n-1}$ with several handwritten annotations in pink:

- An arrow points from the text "nth term" to the variable u_n .
- An arrow points from the text "1st term" to the variable u_1 .
- An arrow points from the text "common ratio (mult.)" to the variable r .
- An arrow points from the text "number of terms" to the exponent $n-1$.

Find the 14th term...

1, 3, 9, 27, ...
3
(14-1)
13

$$14 = 1(3)$$

1, 5, 9, 323

$$a^0 = 1 \quad 3^0(1-1)$$

$$e^0 = 1$$

Challenge: Find the
14th term in the
sequence:

2, -4, 8, -16...

$$u_4 = 2(-2)^{14-1}$$

$$u_4 = 2(-8192)$$

$$u_4 = -16384$$

$$u_n = u_1 r^{n-1}$$

Find the 11th term...

$$u_n = u_1 r^{n-1}$$

300, 150, 75, ...

4 SF
↓

4000

12,000 ← 2 SF

$$u_{11} = 300 (.5)^{11-1}$$

$u_{11} = .293$.406

$$= 0000.293$$

always
multiplic

3 significant figures

- 1-9 are significant
- leading 0's are not significant
- sandwiched 0's are
- trailing 0's are (only after decimal)

Discussion/Challenge topic:

Can a sequence be both arithmetic and geometric?

19, 19, 19, 19, 19, ...

Give an example regardless of your answer.

$$u_n = u_1 r^{n-1}$$

0, 0, 0, 0, 0, ...

$$U_n = U_1 + (n-1)d$$

Arithmetic

Is the following sequence ~~arithmetic~~ or geometric?

$$u_n = u_1 r^{n-1}$$

2, 3, 4.5,
✓

Regardless of your answer, find u_8

common ratio = $\frac{\text{2nd term}}{\text{1st term}}$
 $u_8 = 2(1.5)^{8-1}$

$2(17.086)$

34.2



3 SF or exact

u_8
 ≈ 34.171875

In a geometric sequence, the 10th term is 39,366. the first term is 2. Find "r."

$$\frac{39,366}{2} = \frac{2(r)^9}{2}$$
$${}^9\sqrt{19683} = {}^9\sqrt{r^9}$$
$$r = 3$$

$$u_n = u_1 r^{n-1}$$

$$y_1 = x^9$$

2nd table

$$19683 = x^9$$
$$0 = x^9 - 19683 = y_1$$

x-intercept
root
solutions
zeros

In the arithmetic sequence,

$$u_4 = 42 \text{ \& } u_{36} = -22; \text{ find } d \text{ \& } u_1$$

$$u_n = u_1 + (n - 1)d$$

Consider the sequence 2, 5, 8, 11...

Find n such that $U_n = 110$

$$u_n = u_1 r^{n-1}$$

Consider the infinite geometric sequence $25, 5, 1, 0.2, \dots$

(a) Find the common ratio. $\frac{1}{5} = 0.2$

$$\frac{5}{25}$$

(b) Find

(i) the 10th term;

$$25(0.2)^9 = 1.28 \times 10^{-5}$$

(ii) an expression for the n th term.

$$25(0.2)^{n-1}$$

sci
notation

$$u_n = u_1 r^{n-1}$$

$$.0000128$$

$$1.28 \times 10^{-5}$$

Consider the sequence 2, 5, 8, 11...

Find n such that $U_n = 110$

$$u_n = u_1 r^{n-1}$$

$$u_n = u_1 + (n - 1)d$$

