

NAME: _____

DATE: 09/20B-21A/2017

ASSIGNMENT: Vectors Create Polygons

[SL-calc]

Magnitude of a vector	$ \mathbf{v} = \sqrt{v_1^2 + v_2^2 + v_3^2}$
Scalar product	$\mathbf{v} \cdot \mathbf{w} = \mathbf{v} \mathbf{w} \cos\theta$ $\mathbf{v} \cdot \mathbf{w} = v_1w_1 + v_2w_2 + v_3w_3$
Angle between two vectors	$\cos\theta = \frac{\mathbf{v} \cdot \mathbf{w}}{ \mathbf{v} \mathbf{w} }$
Vector equation of a line	$\mathbf{r} = \mathbf{a} + t\mathbf{b}$

21.) The diagram shows a parallelogram ABCD.

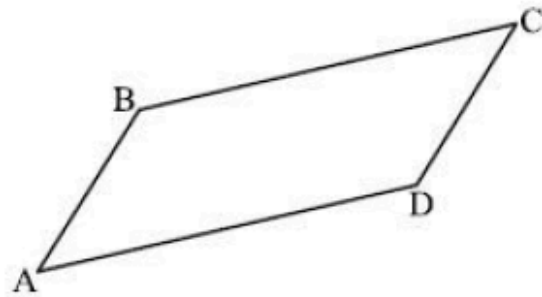


diagram not to scale

The coordinates of A, B and D are A(1, 2, 3), B(6, 4, 4) and D(2, 5, 5).

- (a) (i) Show that $\overrightarrow{AB} = \begin{pmatrix} 5 \\ 2 \\ 1 \end{pmatrix}$.
- (ii) Find \overrightarrow{AD} .
- (iii) Hence show that $\overrightarrow{AC} = \begin{pmatrix} 6 \\ 5 \\ 3 \end{pmatrix}$.
- (b) Find the coordinates of point C.
- (c) (i) Find $\overrightarrow{AB} \bullet \overrightarrow{AD}$.
- (ii) Hence find angle A.
- (d) Hence, or otherwise, find the area of the parallelogram.

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Answer key (show all calculations for full marks)

$$AD = \frac{1}{\frac{3}{2}}$$

Point C = (7, 7, 6)

$$\frac{13}{\sqrt{30} * \sqrt{14}}$$

Arccosine will find the angle

$$\text{Area} = 15.8 = 0.5(a*b*\sin C)$$